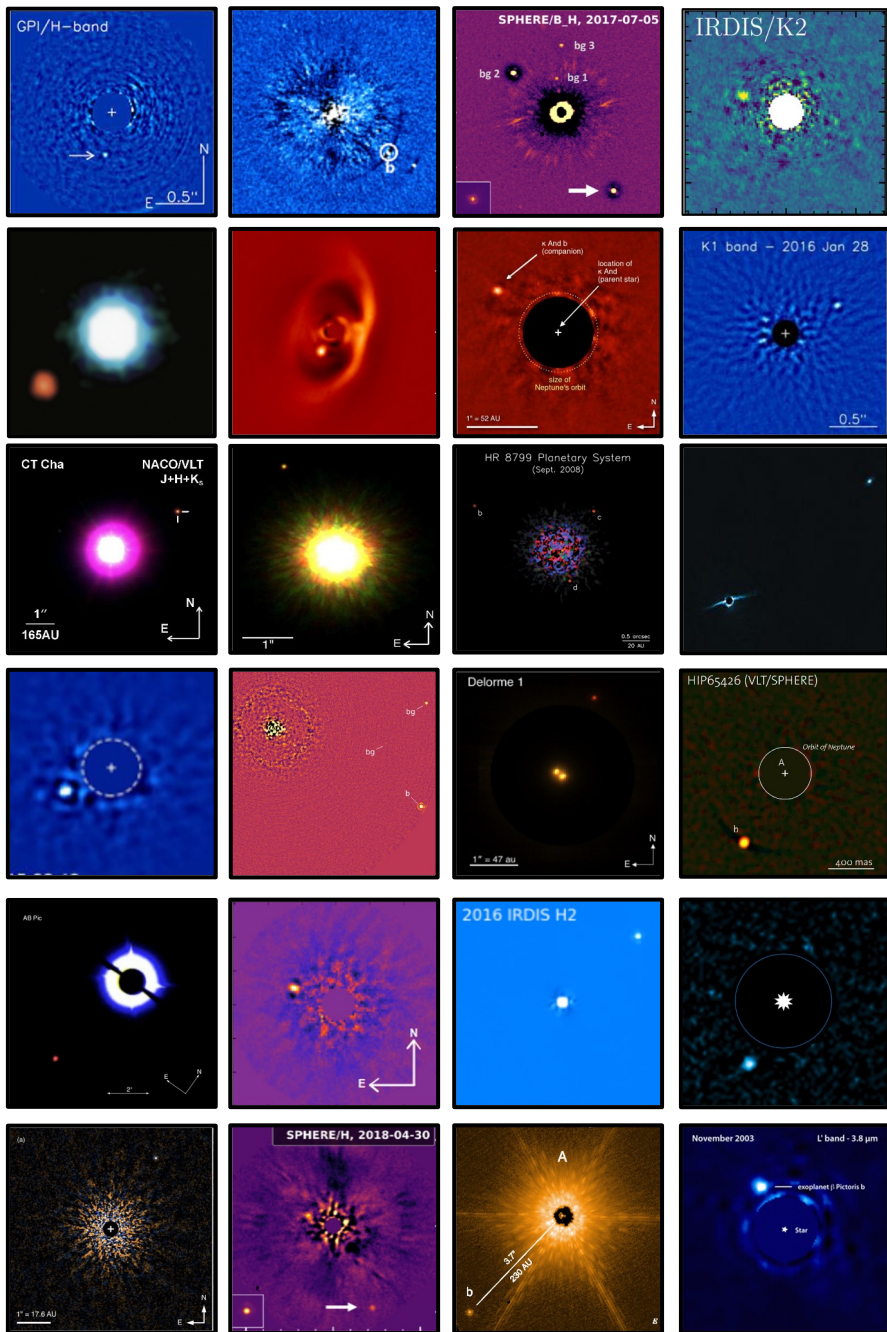
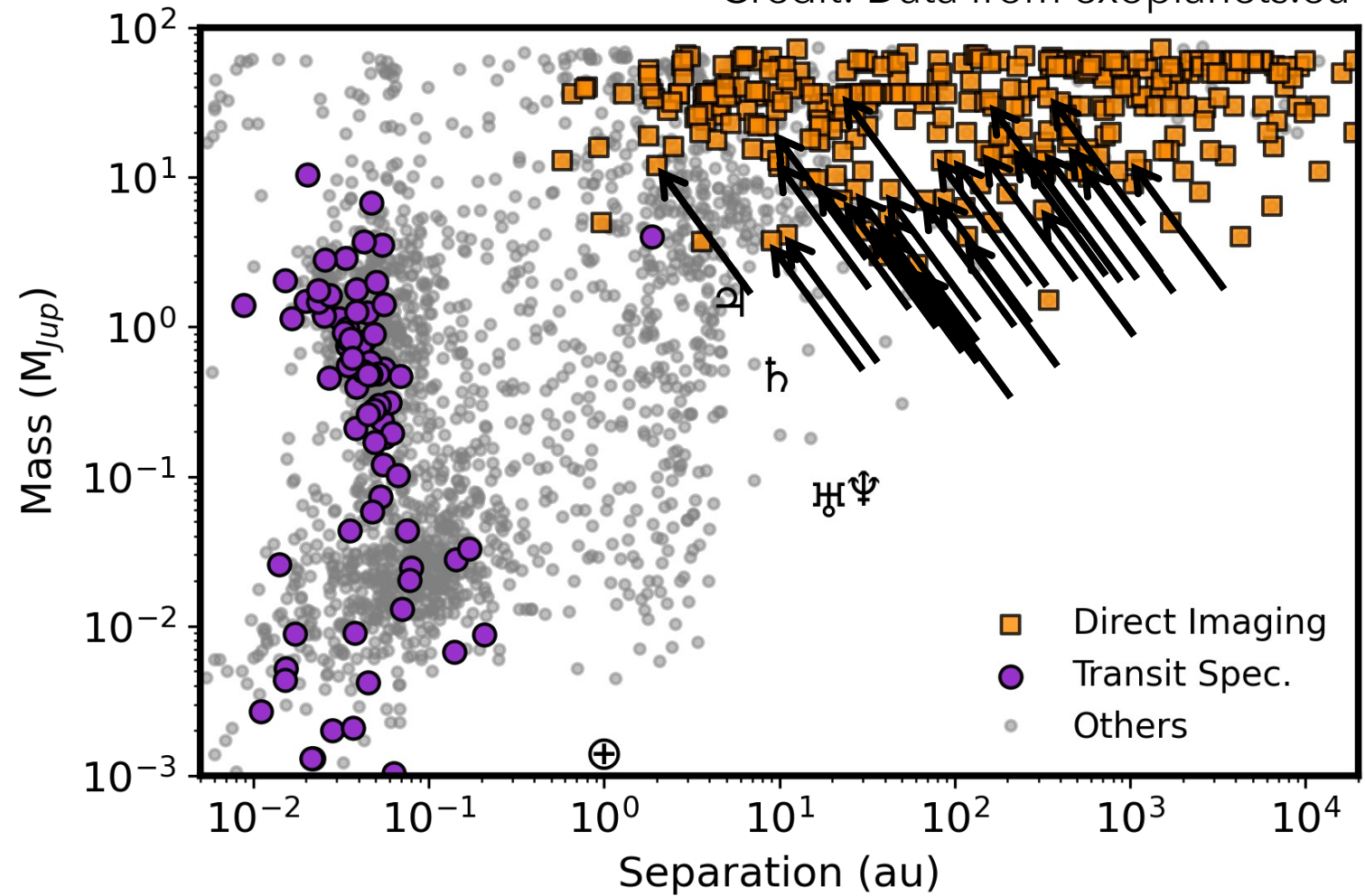


## Atmospheric retrievals with optimal estimation

**Paulina Palma-Bifani**, Benjamin Charnay, Jeremy Leconte, Alice Radcliffe, Bruno Bezard, et al.

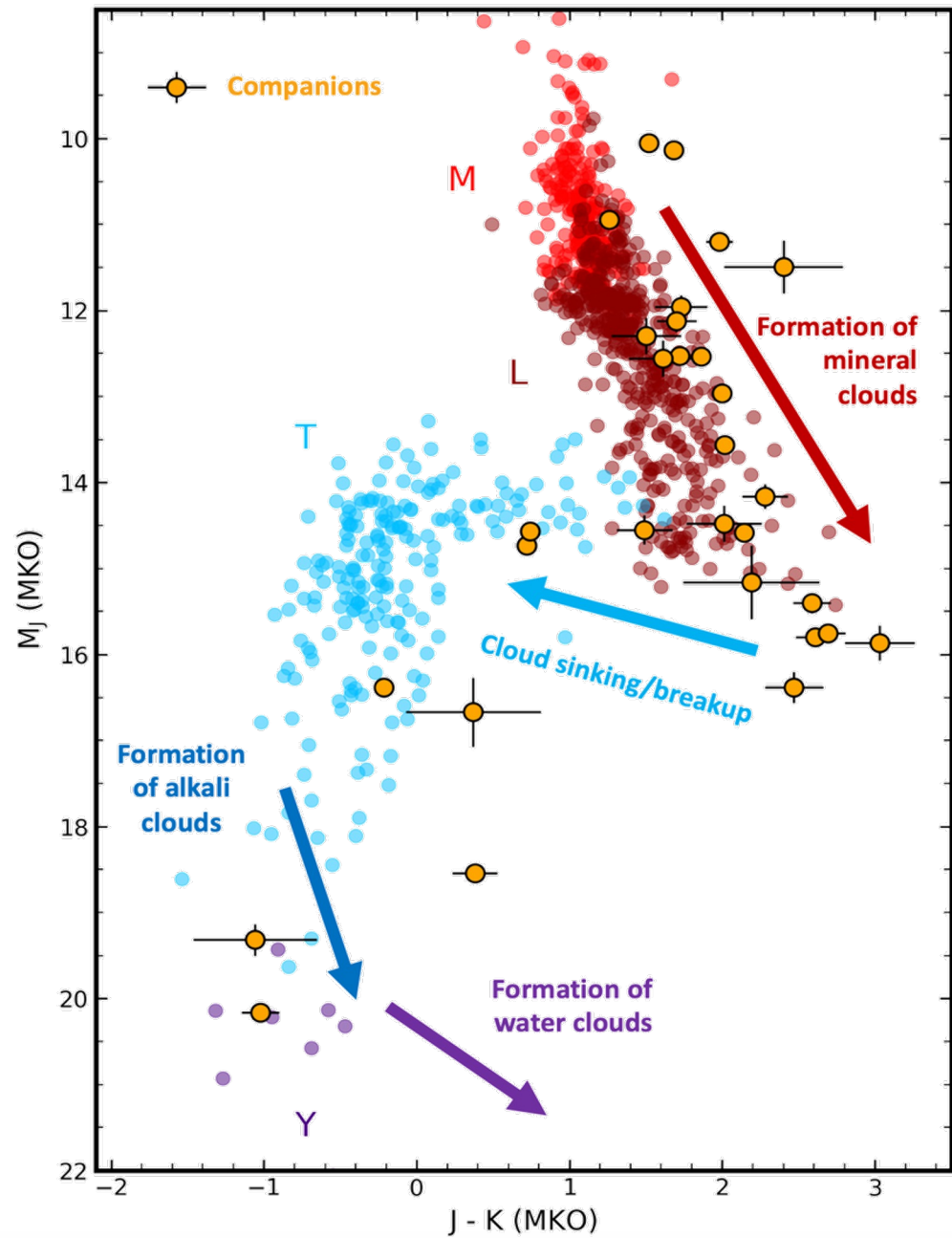


Credit: Data from exoplanets.eu

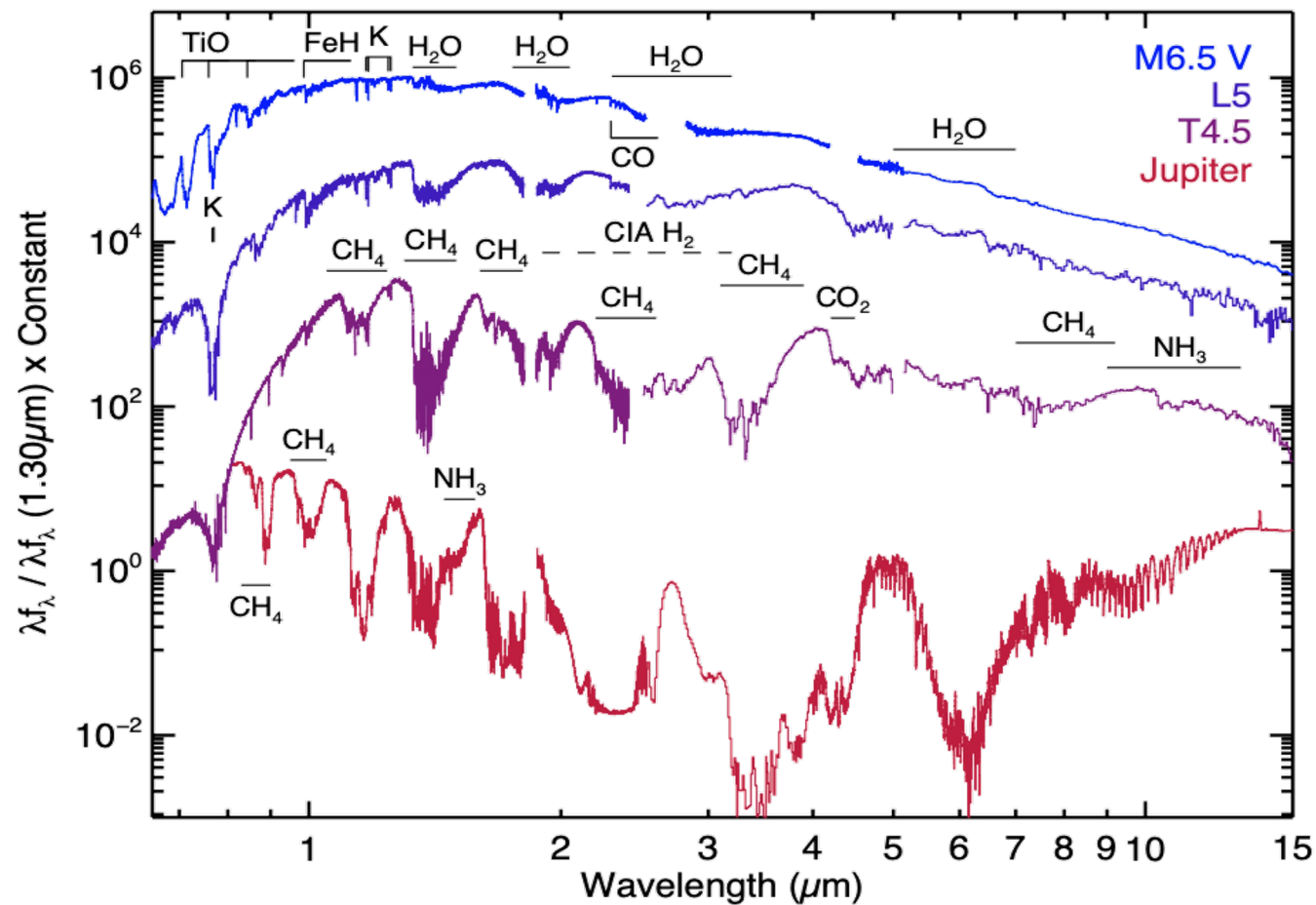
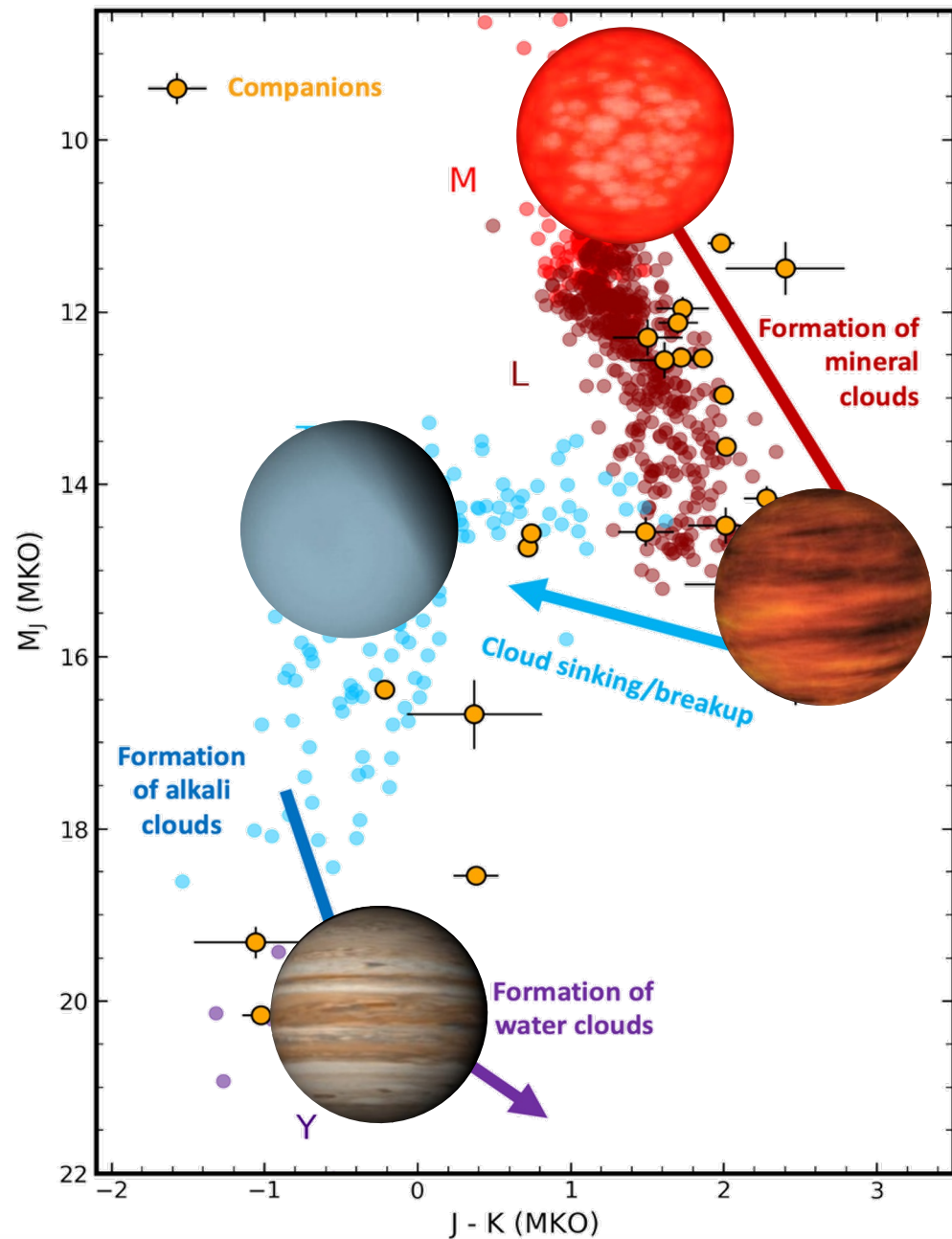


Chauvin et al. (2004, 2005, 2017), Macintosh et al. (2015),  
 Lafrenière et al. (2008), Keppler et al. (2018),  
 Marois et al. (2008, 2010), Cheetham et al. (2018),  
 Lagrange et al. (2019), Milli et al. (2017),  
 Nowak et al. (2019), Wagner et al. (2021),  
 Rameau et al. (2013), Squicciarini et al. (2022),  
 Kurzawa et al. (2013), Janson et al. (2019, 2021),  
 Delorme et al. (2012), Bohn et al. (2020, 2021a, 2021b),  
 Bailey et al. (2012), de Rosa et al. (2023)

Credit: Gao et al. (2021)

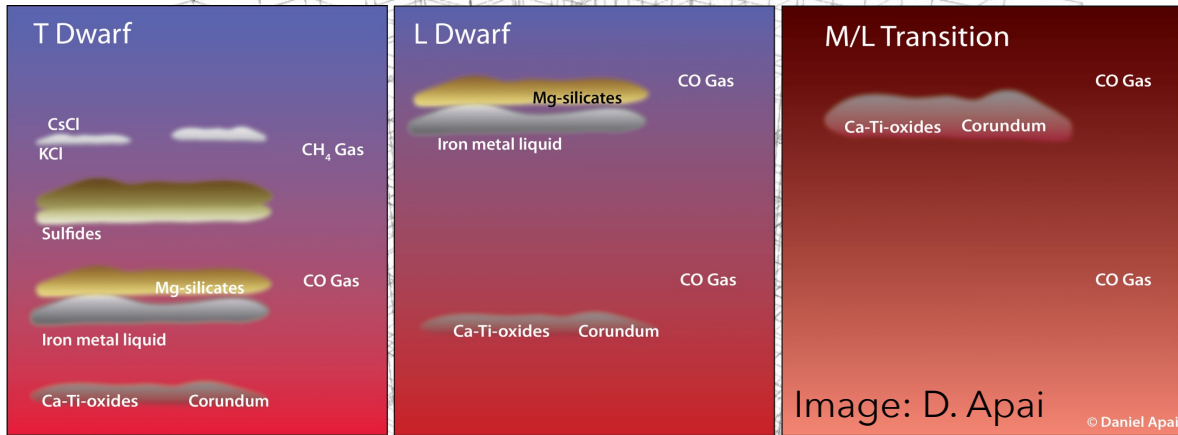


Credit: Gao et al. (2021)



Credit: J. Fortney (2018)

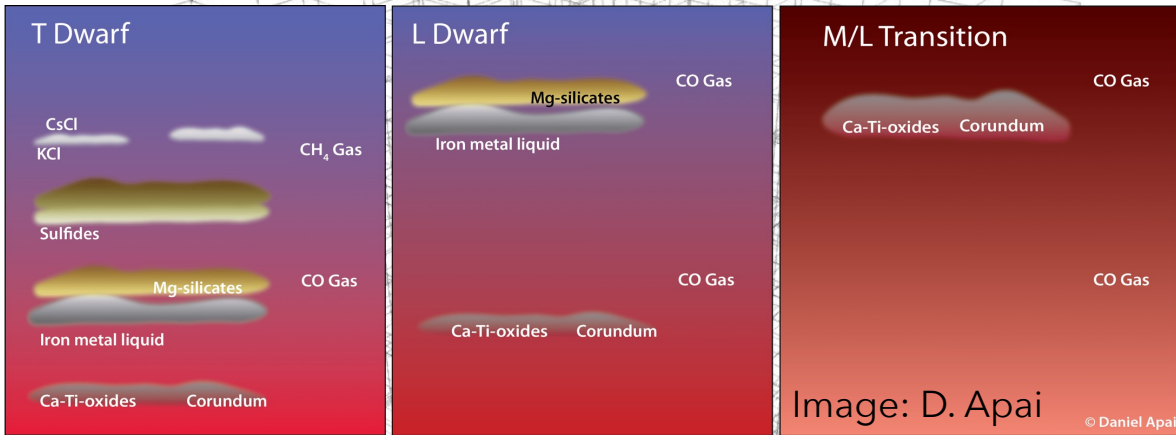
# Atmospheric parametrizations of self consistent models:



**Temperature**  
**Surface gravity**  
**Metallicity ([M/H])**  
**Abundances ( $X_A/X_B$ )**  
**Clouds, ...**

Grids: Exo-REM, Sonora, BT-Settl, ATMO, ...

# Atmospheric parametrizations of self consistent models:

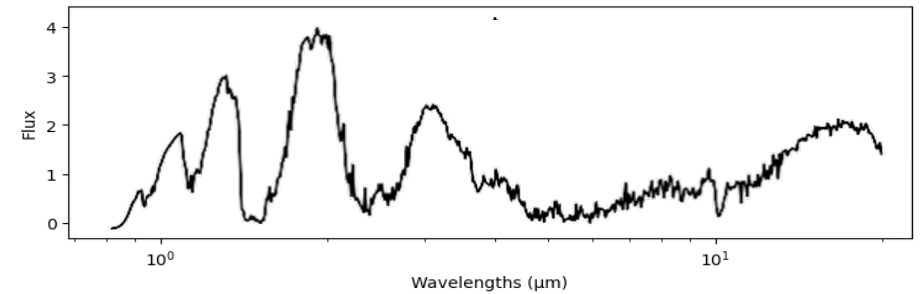
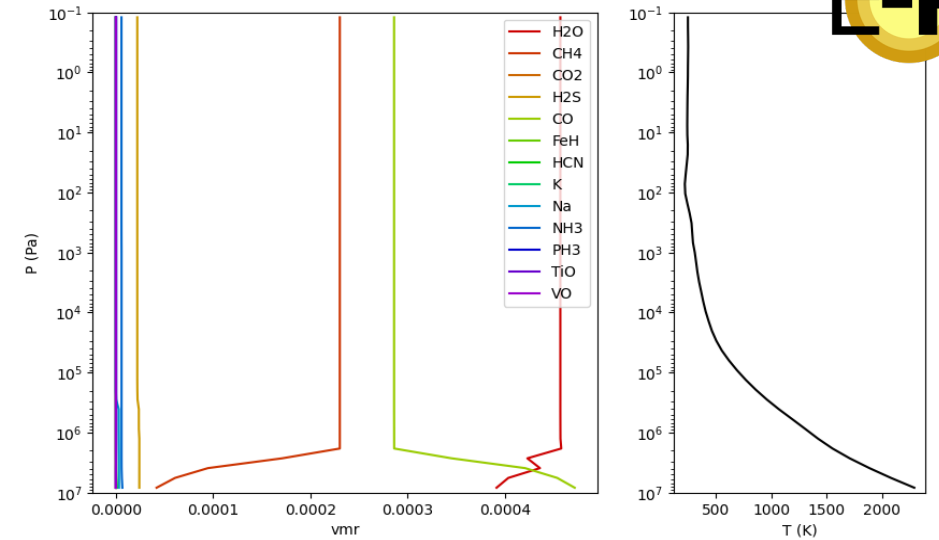


Temperature  
 Surface gravity  
 Metallicity ( $[M/H]$ )  
 Abundances ( $X_A/X_B$ )  
 Clouds, ...

Grids: Exo-REM, Sonora, BT-Settl, ATMO, ...

## Exo-REM k26

(Radcliffe et al. 2026)



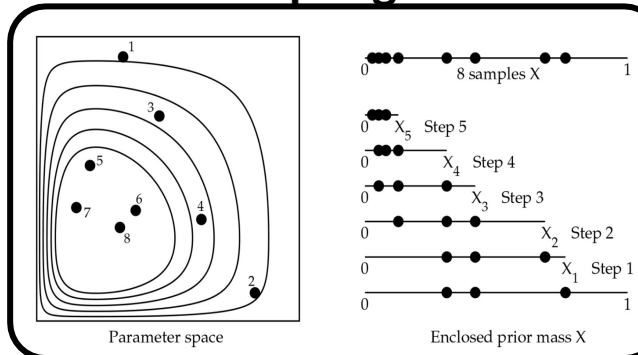
# How to use these models to analyze observations?

*Bayesian framework*

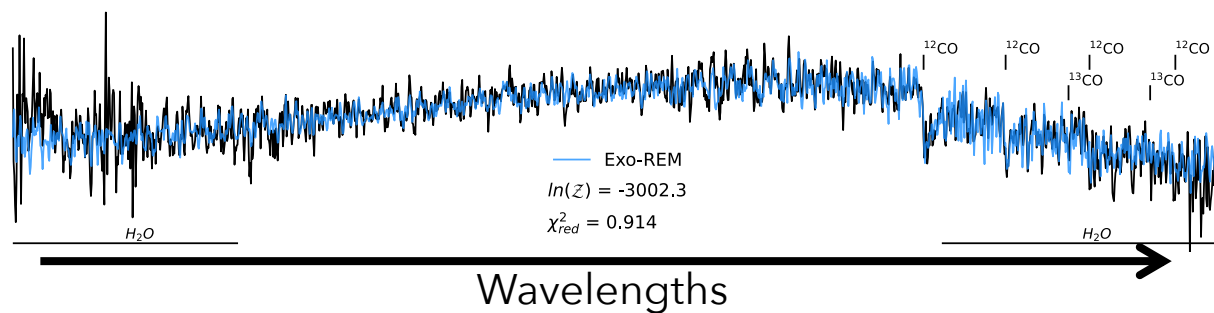
$$P(y|x)P(x) = P(x|y)P(y)$$

# Forward modeling with ForMoSA:

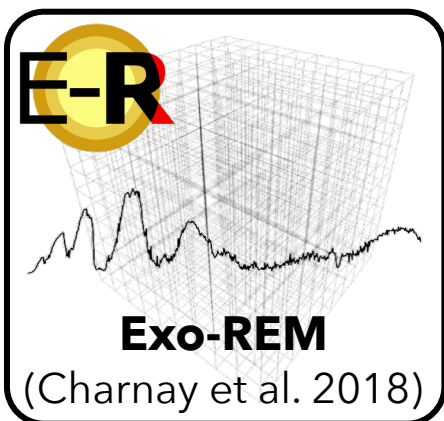
## Nested Sampling:



Exo-REM model of  $\beta$  Pic b VLT/GRAVITY+ observations  
Ravet et al. (2025)



Self-consistent atmospheric model:

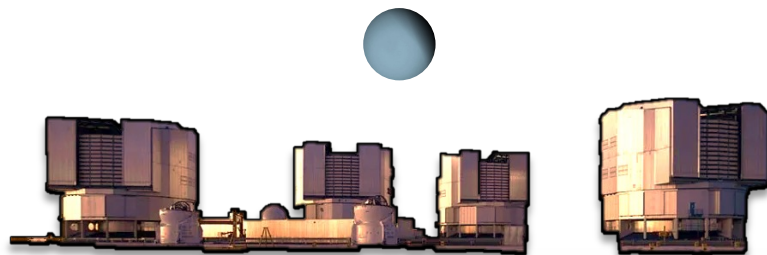


Free parameters include:

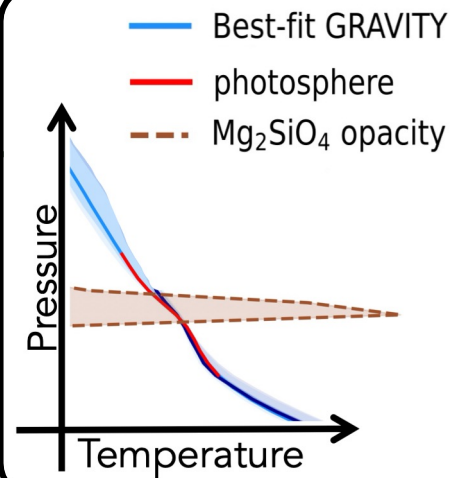
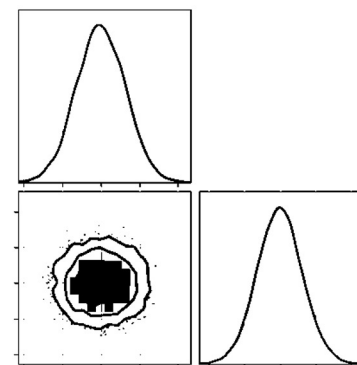
$T_{eff}, \log(g), [M/H], C/O, f_{sed}, R, d, RV, v \sin(i), \dots$

Observation:

$\beta$  Pic b with VLT/GRAVITY+



Corner plot

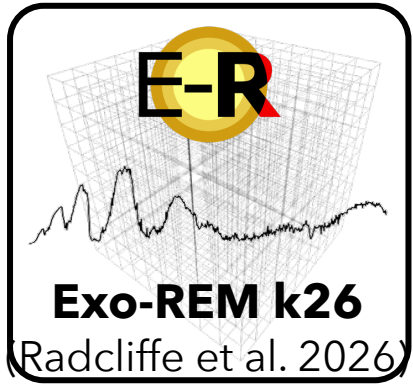


# Forward modeling with ForMoSA:



- **Robust framework:** Grids based on self-consistent models
- **Statistical flexibility:** Multi-metric likelihoods tailored to the dataset
- **Comprehensive parameters:** Grid properties,  $d$ ,  $R$ ,  $v\sin(i)$ ,  $RV$ , scaling, and CPDs
- **Wide exploration:** Efficient global mapping across extensive parameter ranges

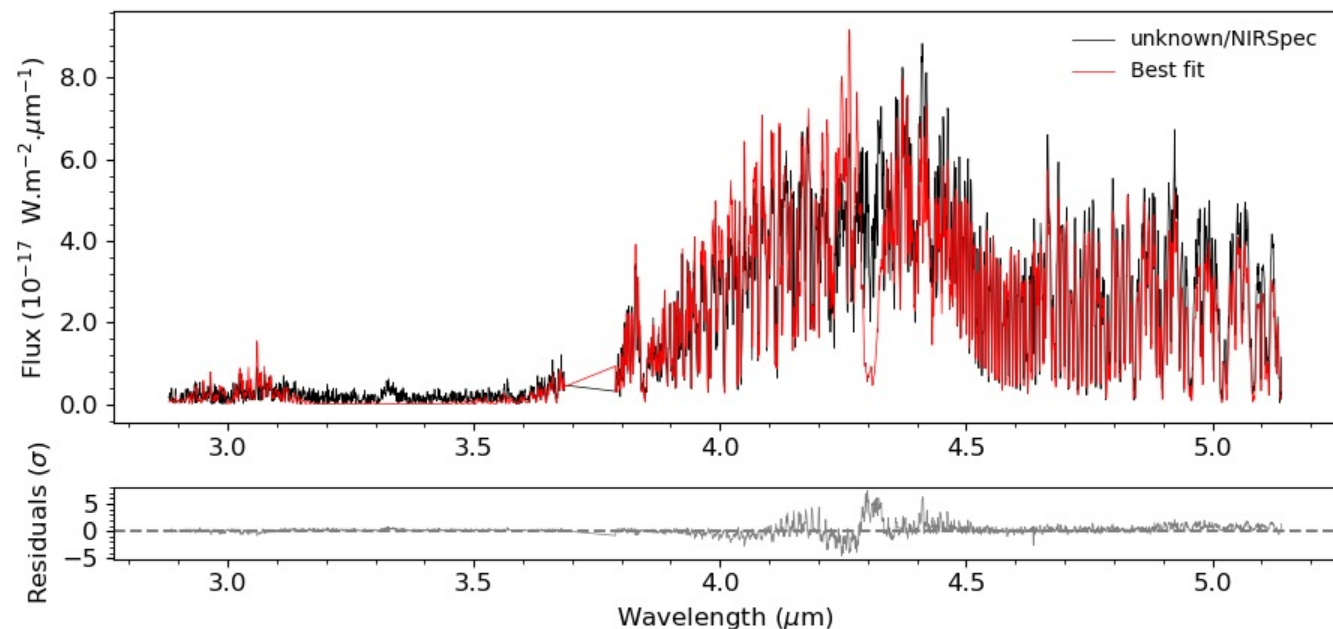
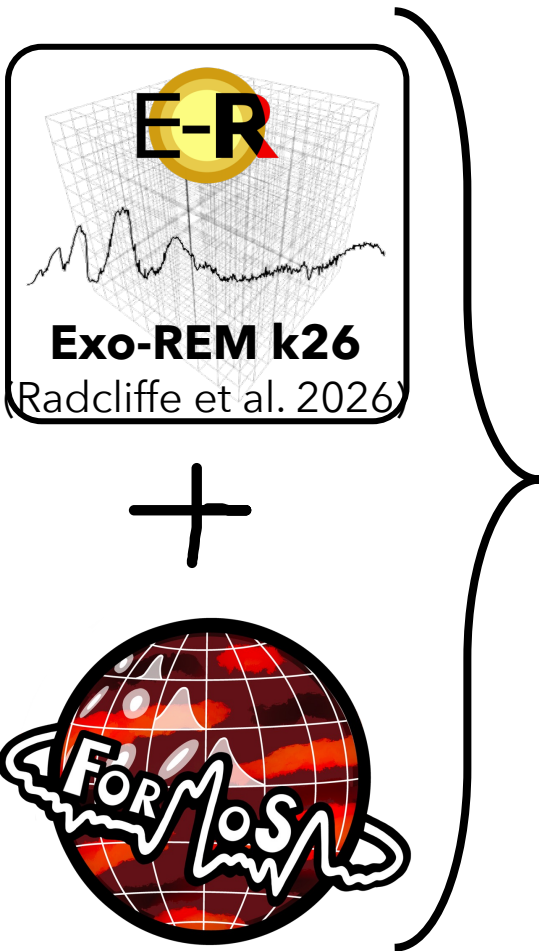
# W1935



+



# W1935



Parameters  $\pm 1\sigma$

**Teff** =  $407.6 \pm 0.7$

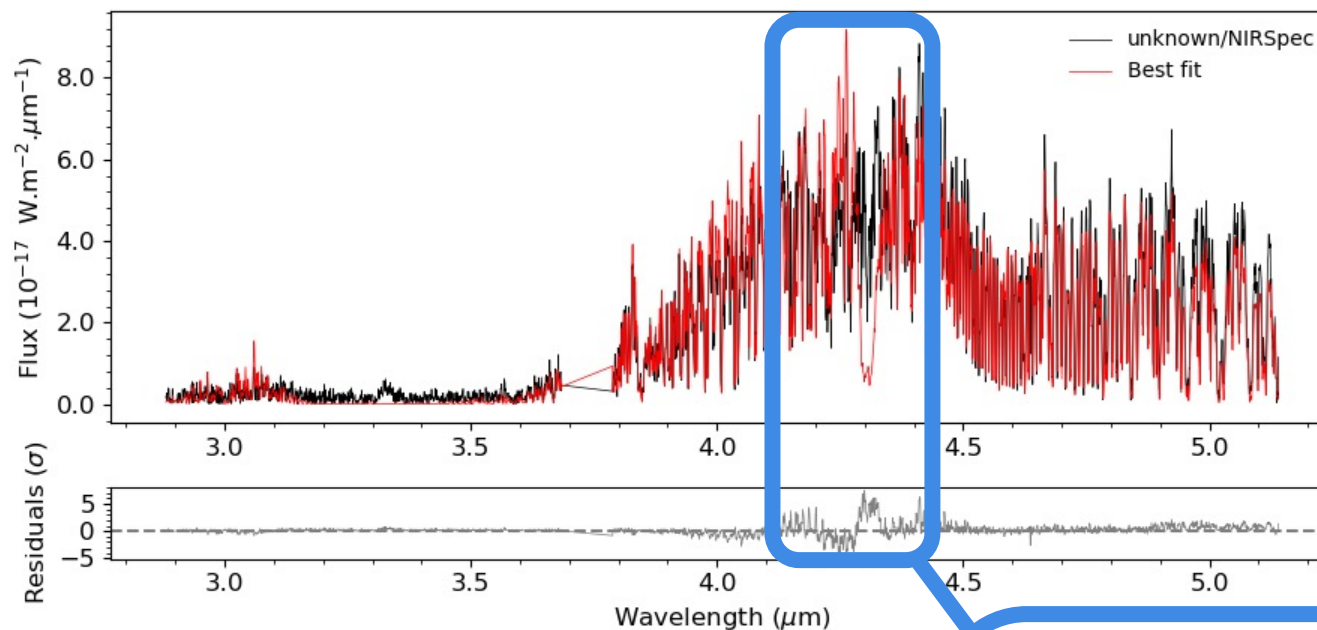
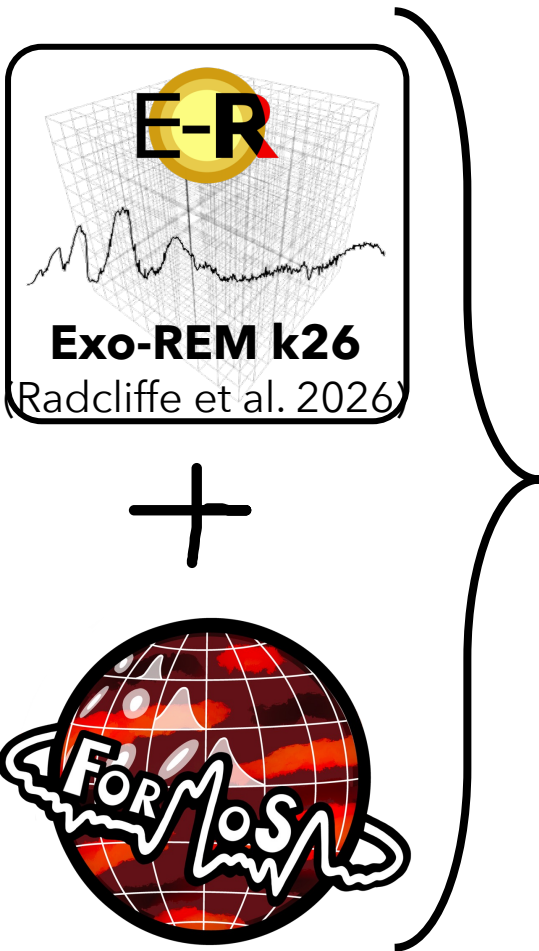
**log(g)** =  $4.60 \pm 0.01$

**[M/H]** =  $-0.33 \pm 0.01$

**C/O** =  $0.8 \pm 0.0003$

**r** =  $1.37 \pm 0.01$

# W1935



Parameters  $\pm 1\sigma$

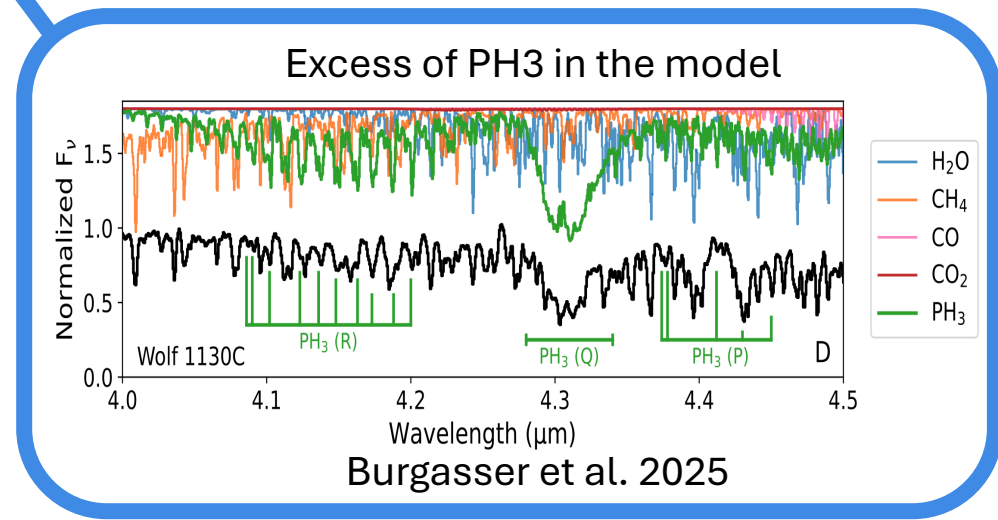
**Teff** =  $407.6 \pm 0.7$

**log(g)** =  $4.60 \pm 0.01$

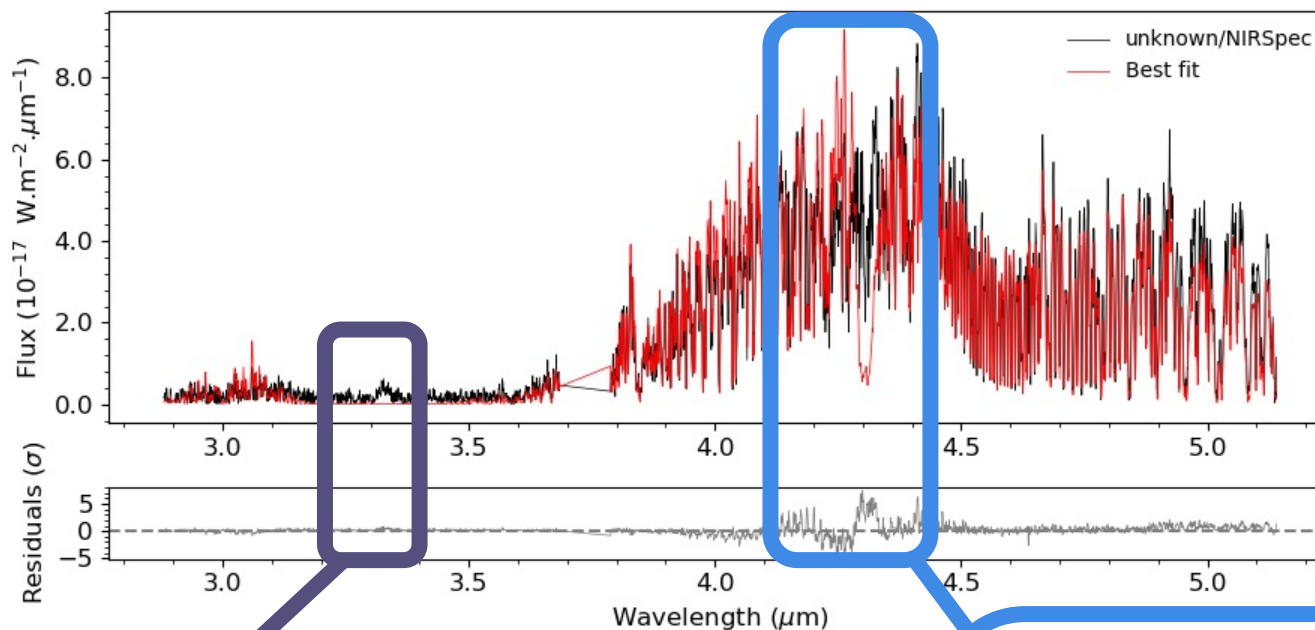
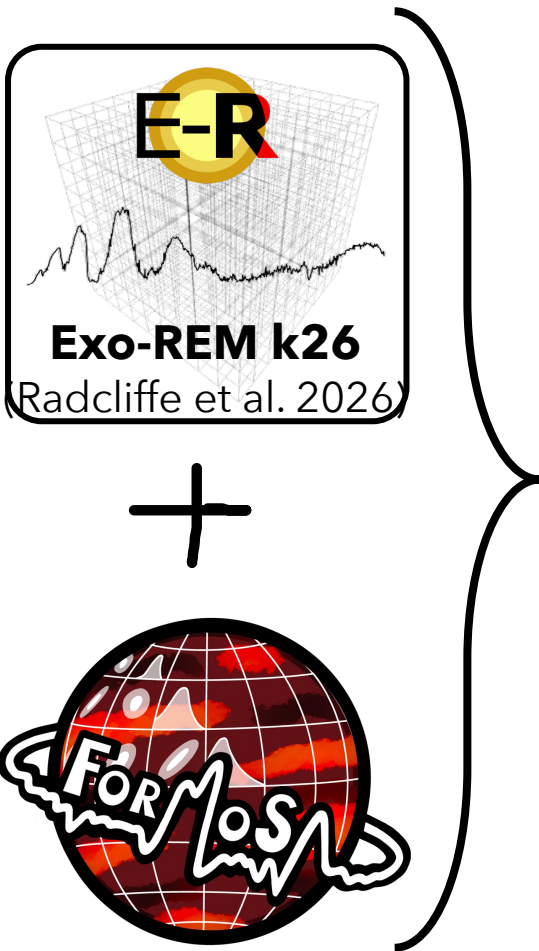
**[M/H]** =  $-0.33 \pm 0.01$

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# W1935



Parameters  $\pm 1\sigma$

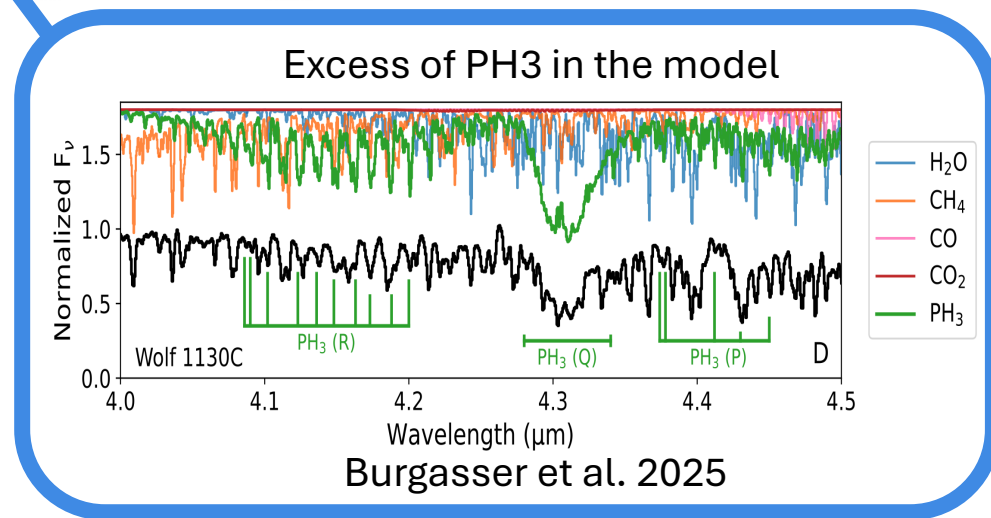
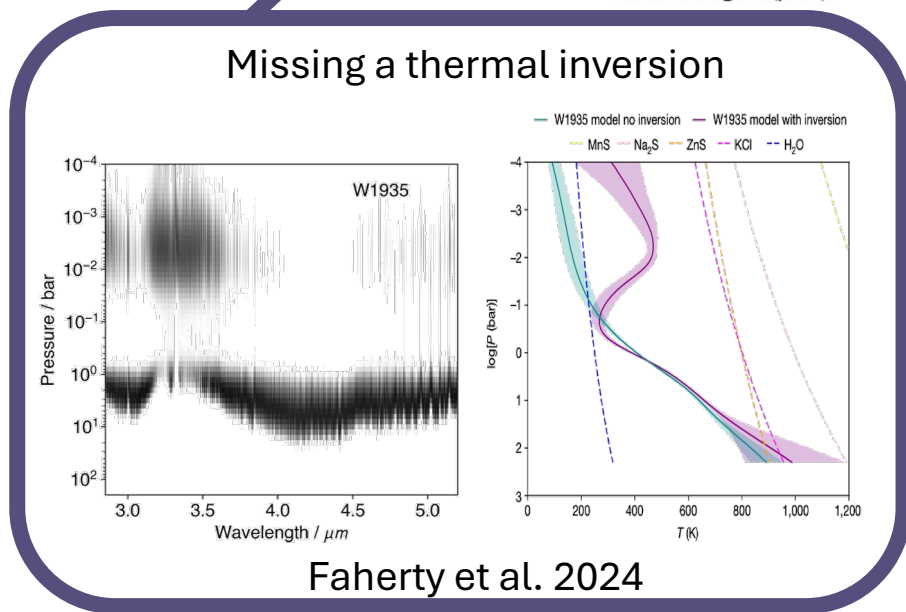
**Teff** =  $407.6 \pm 0.7$

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**[M/H]** =  $-0.33 \pm 0.01$

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**r** =  $1.37 \pm 0.01$

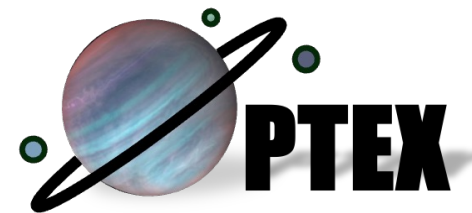


# Forward modeling with ForMoSA:



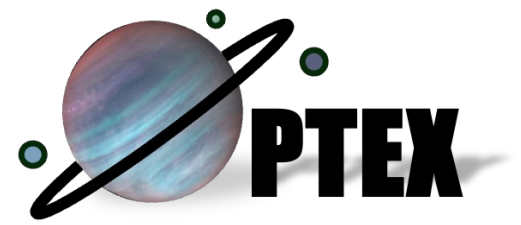
- **Robust framework:** Grids based on self-consistent models
- **Statistical flexibility:** Multi-metric likelihoods tailored to the dataset
- **Comprehensive parameters:** Grid properties,  $d$ ,  $R$ ,  $v\sin(i)$ ,  $RV$ , scaling, and CPDs
- **Wide exploration:** Efficient global mapping across extensive parameter ranges

- **Rigid chemistry:** Tied to pre-computed grids (inflexible)
- **Limited dynamics:** Cannot model complex/localized physics (e.g., aurora-induced thermal inversions)



# Retrievals with optimal estimation:

$$\widehat{x}_k = x_a + G(y - F(x_a))$$

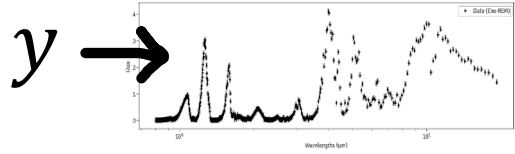
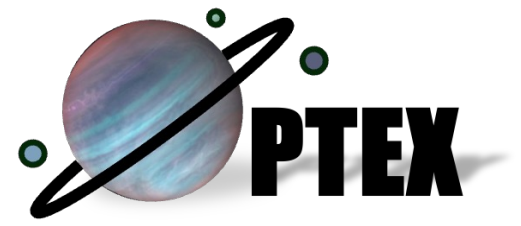


*“A classical Earth and solar system method,  
~100× faster than nested sampling free retrievals.”*

Based on Rodgers (2000)

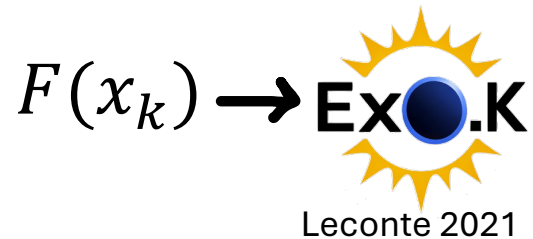
# Retrievals with optimal estimation:

$$\widehat{x}_k = x_a + G(y - F(x_a))$$



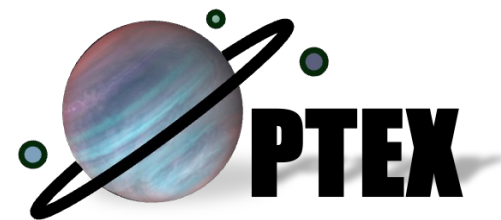
$x_k$  →

$$\begin{pmatrix} T_1 \\ T_2 \\ \dots \\ T_{15} \\ \log(g) \\ H_2O \\ CH_4 \\ CO \\ \dots \end{pmatrix}_k$$

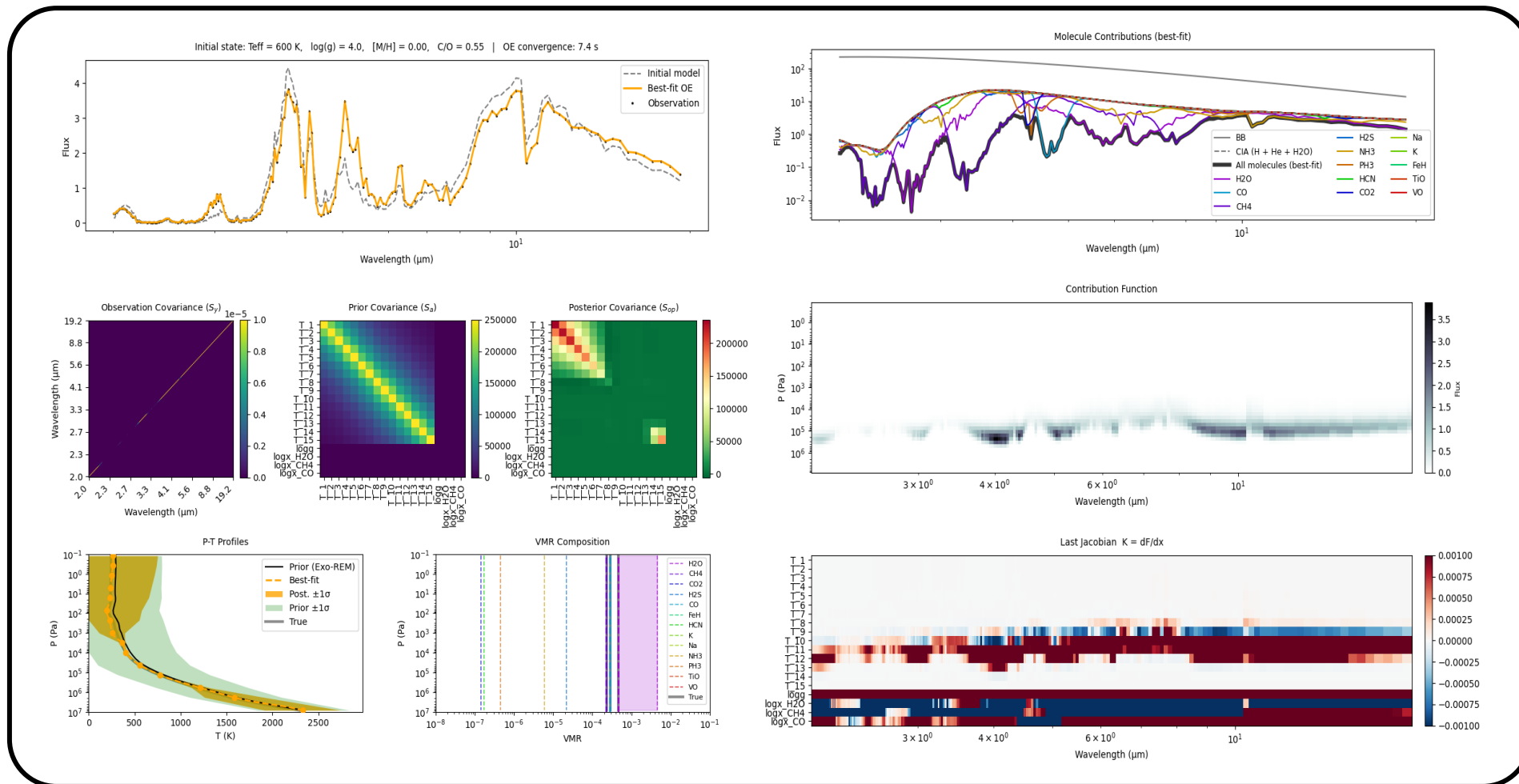
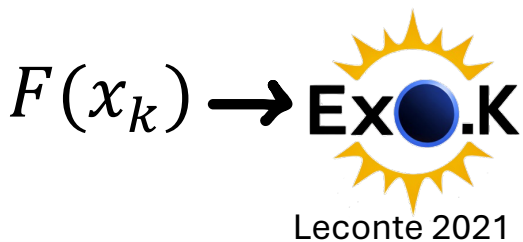
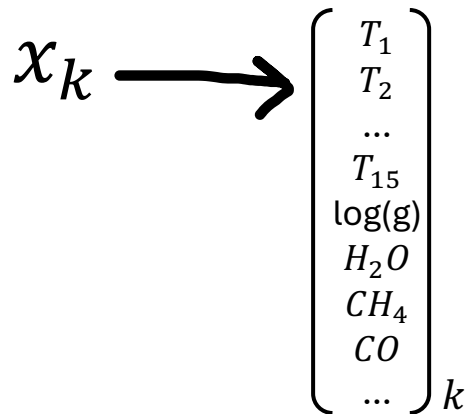
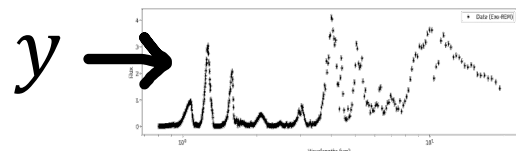


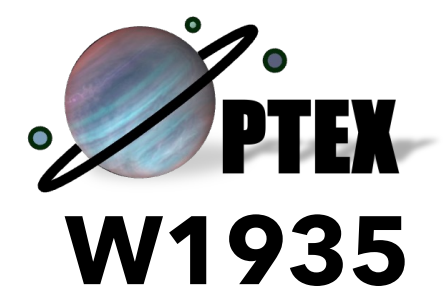
# Retrievals with optimal estimation:

$$\widehat{x}_k = x_a + G(y - F(x_a))$$



Validation demo results:

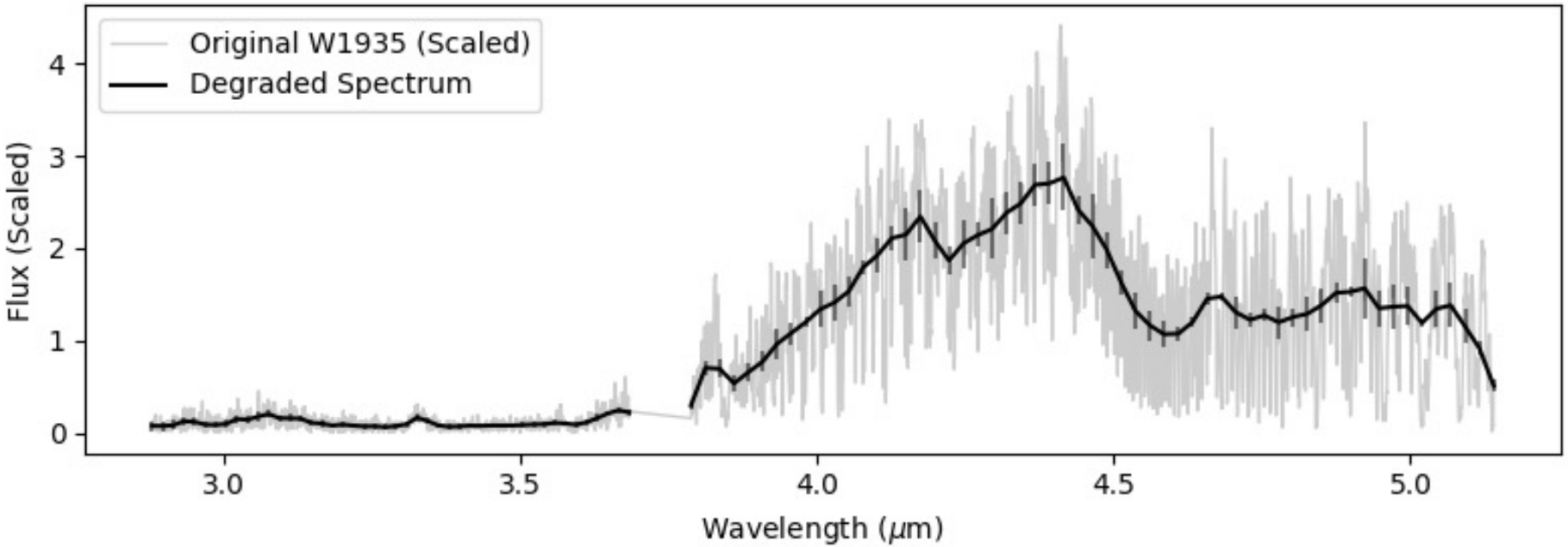




**Preliminary results :**  
*Retrieving a thermal inversion ...*

# Preliminary results :

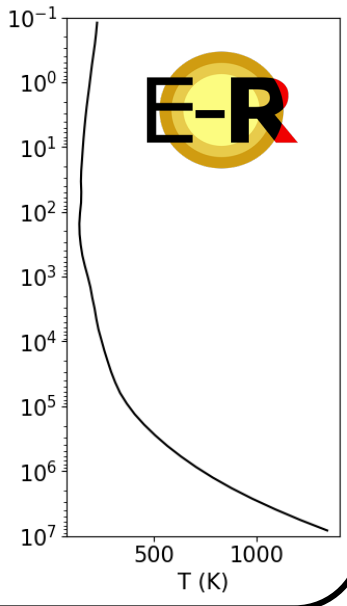
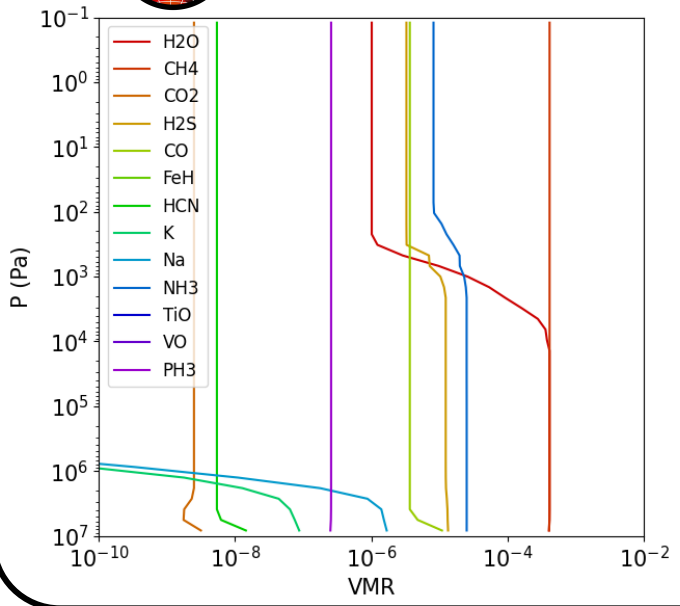
*Retrieving a thermal inversion ...*




# PTEX W1935



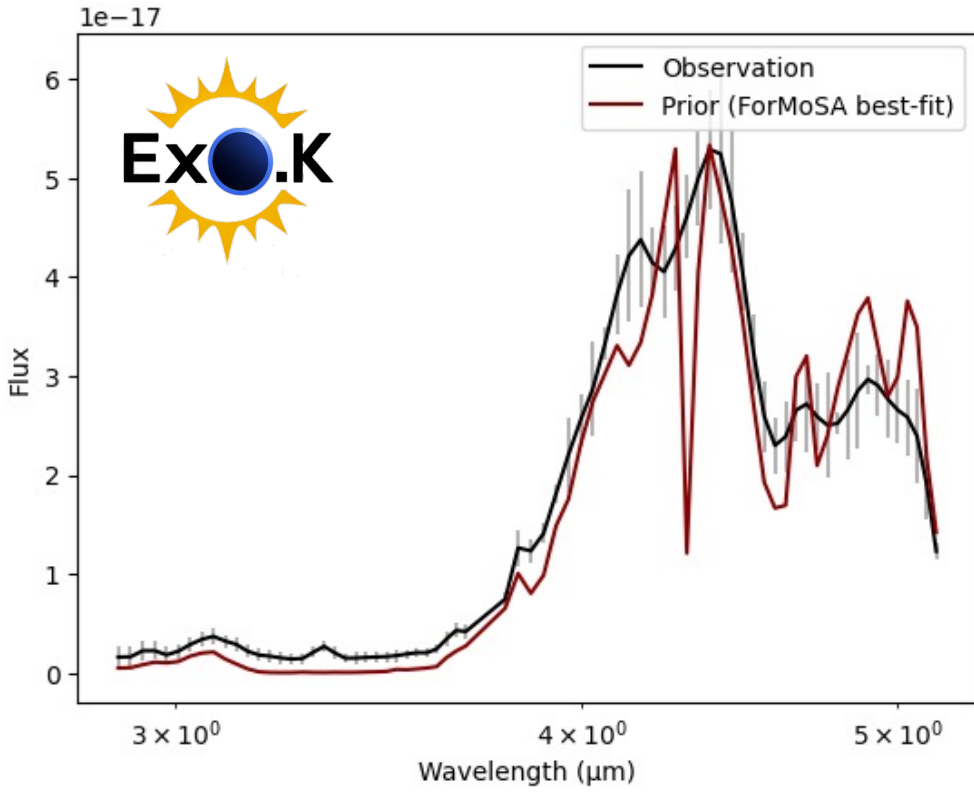
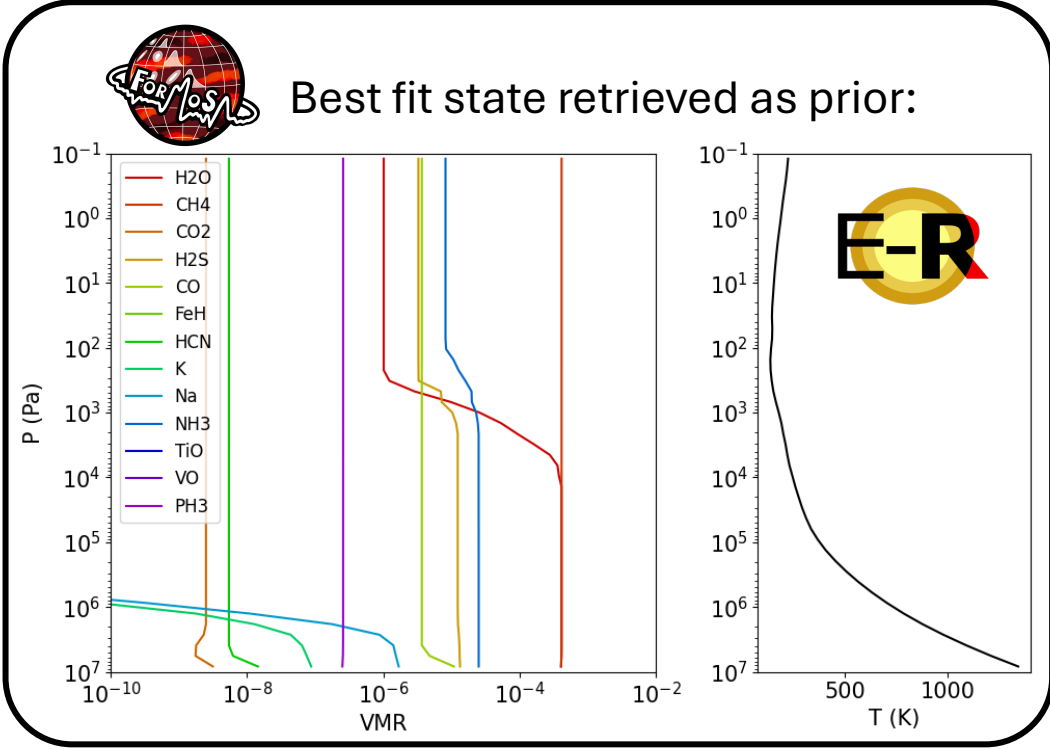
Best fit state retrieved as prior:



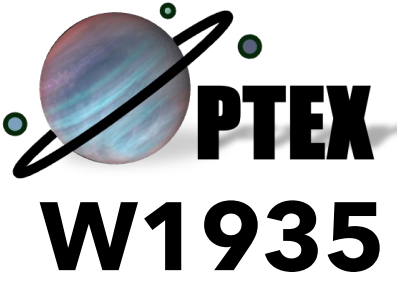


# PTEx

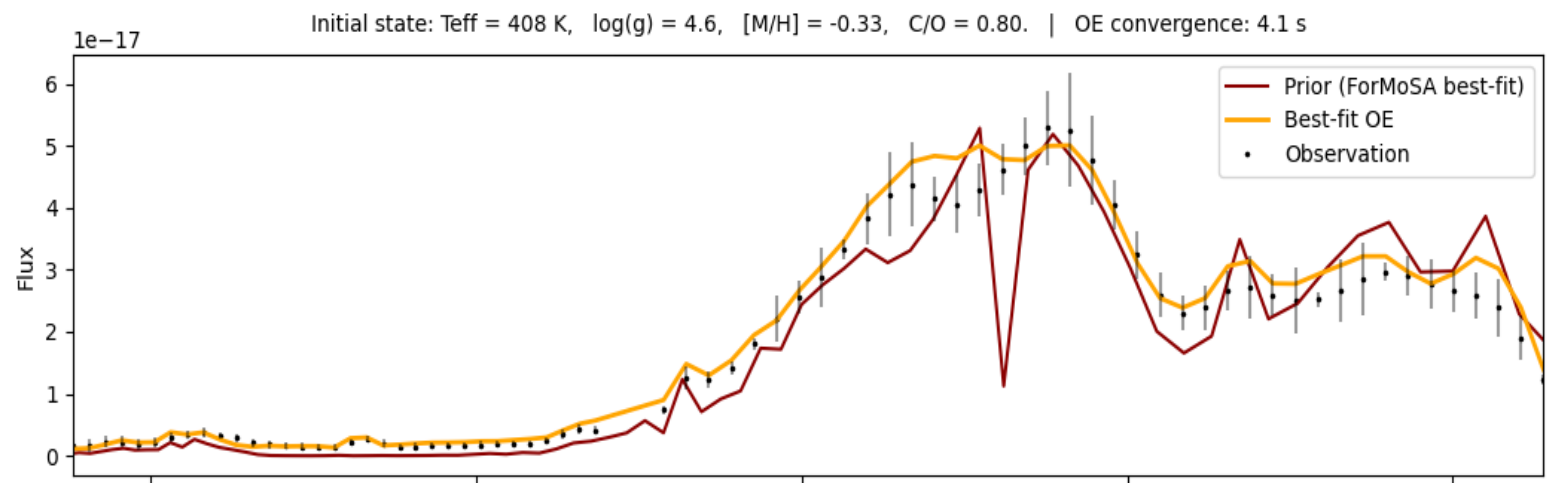
## W1935

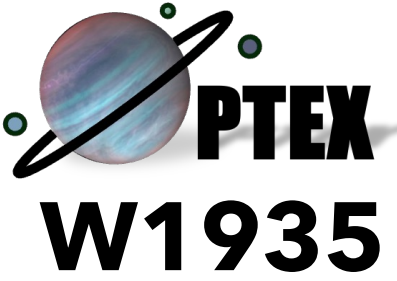


- 
- $T_1$
  - $T_2$
  - ...
  - $T_{15}$
  - $\log(g)$
  - H<sub>2</sub>O
  - CH<sub>4</sub>
  - CO
  - ...
- $k$

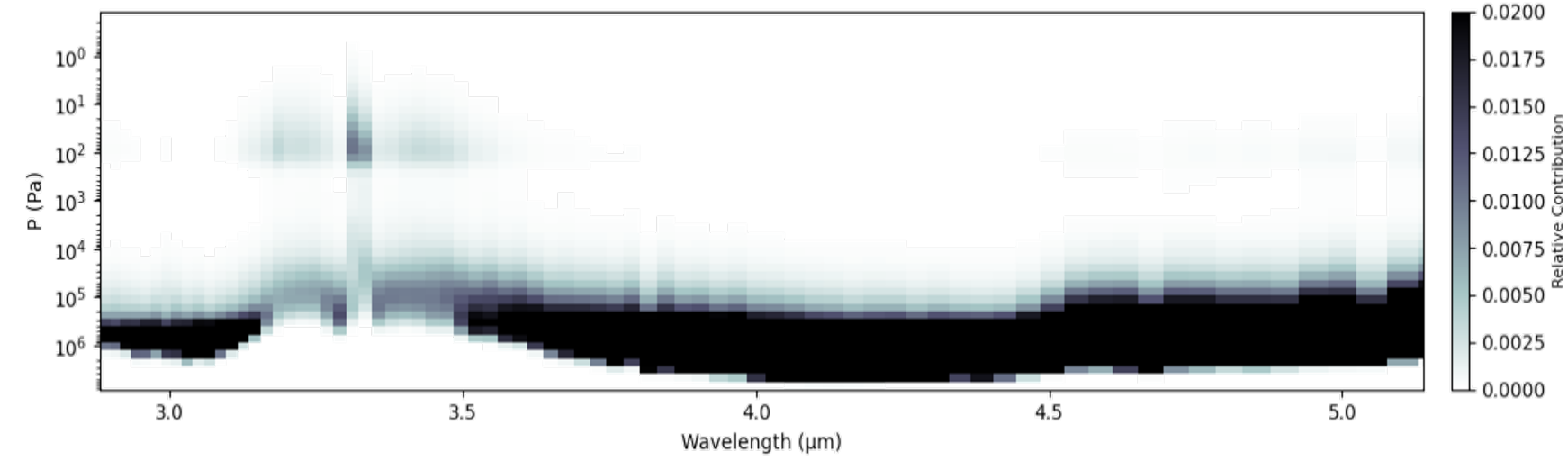
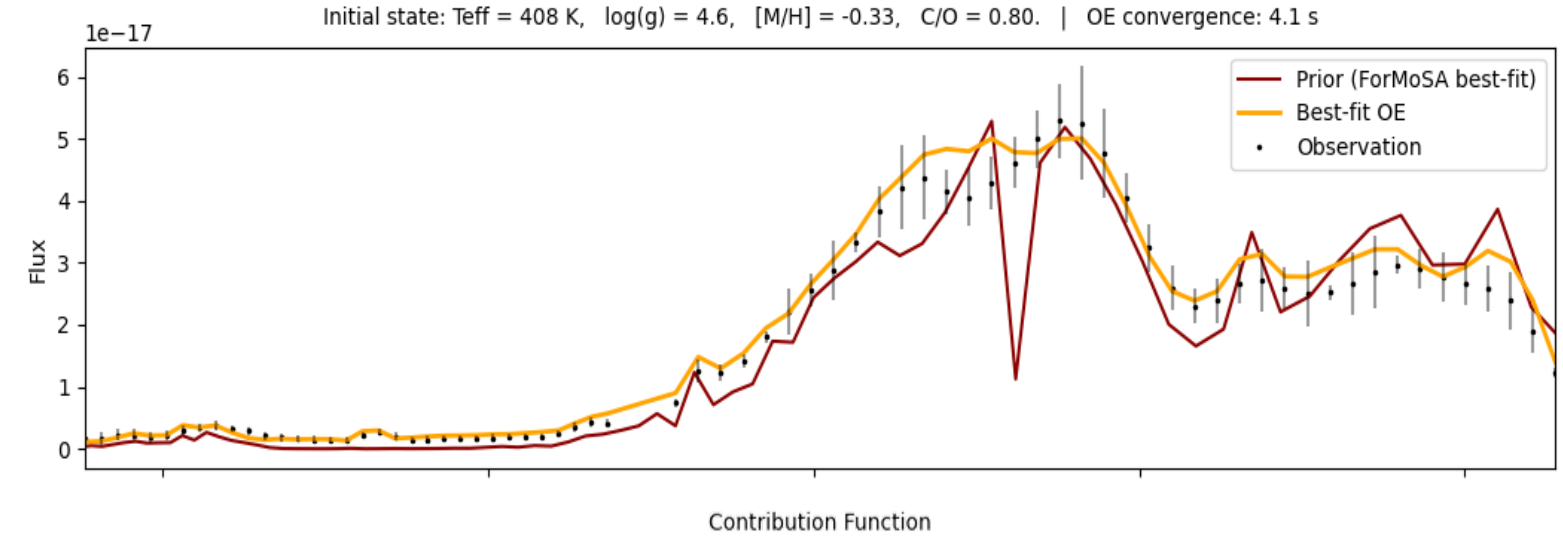


**PTEx**  
**W1935**





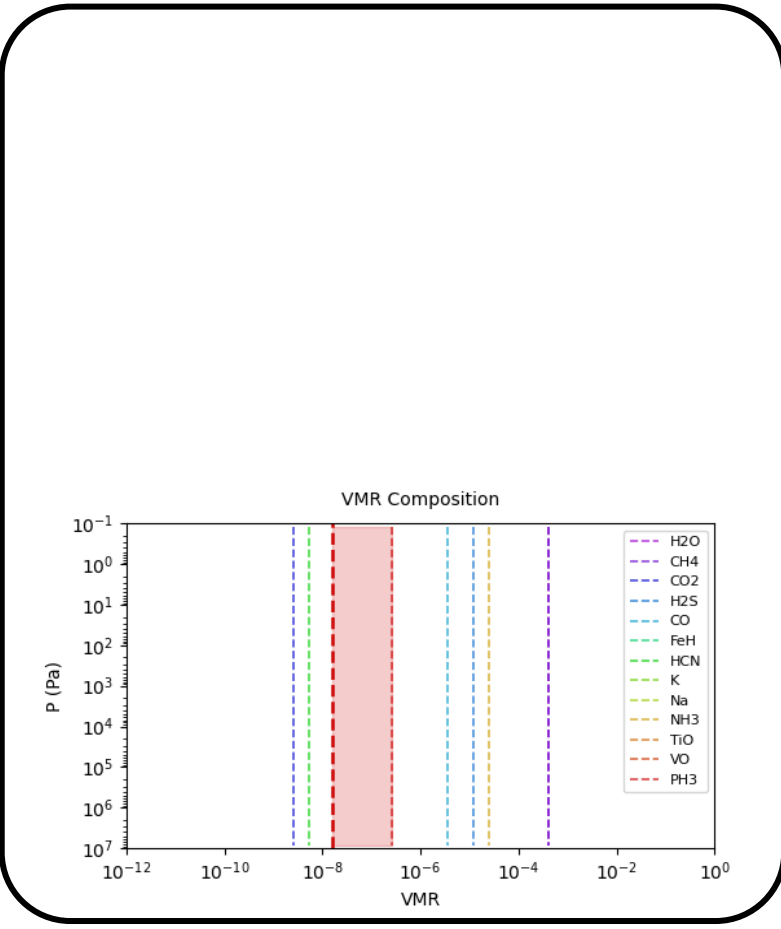
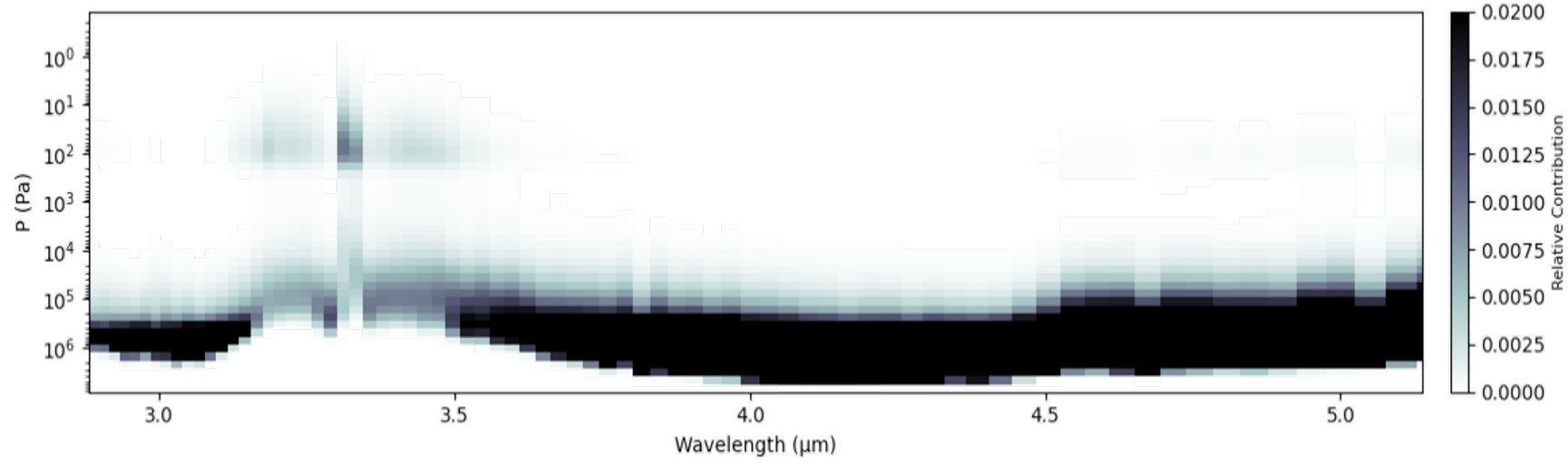
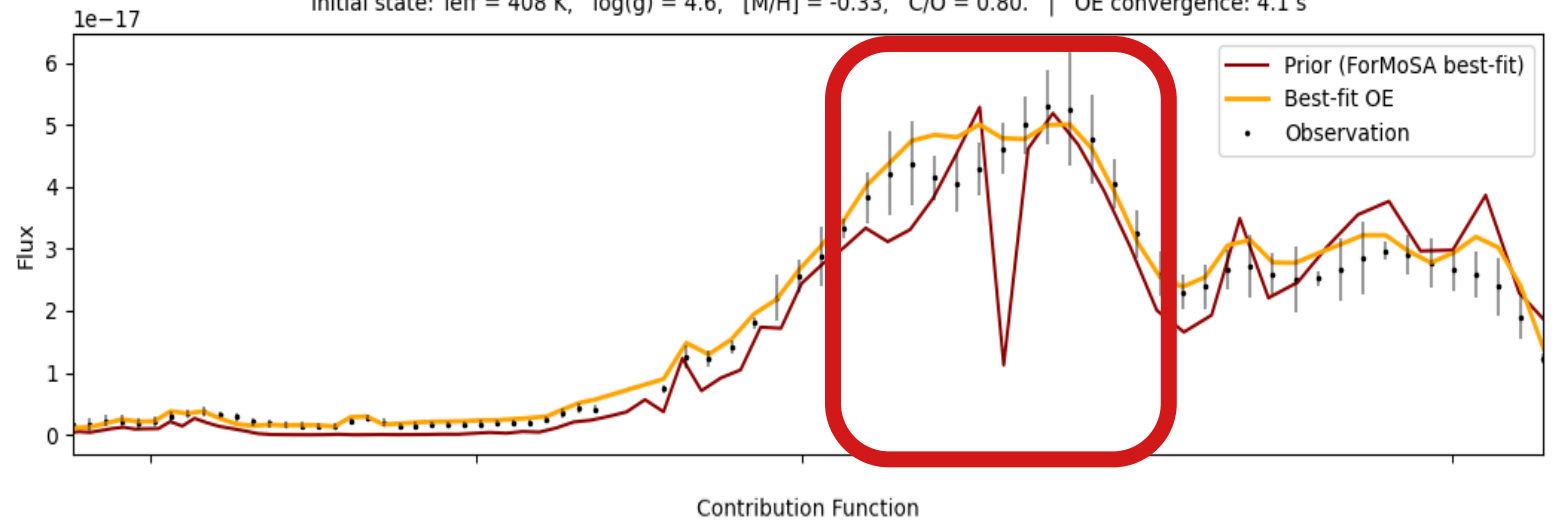
**PTEx**  
**W1935**

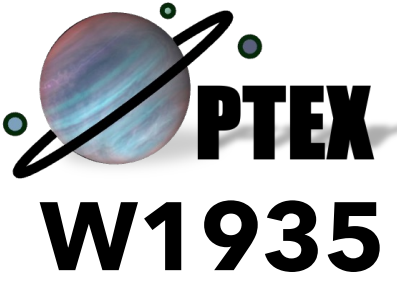




# PTEx W1935

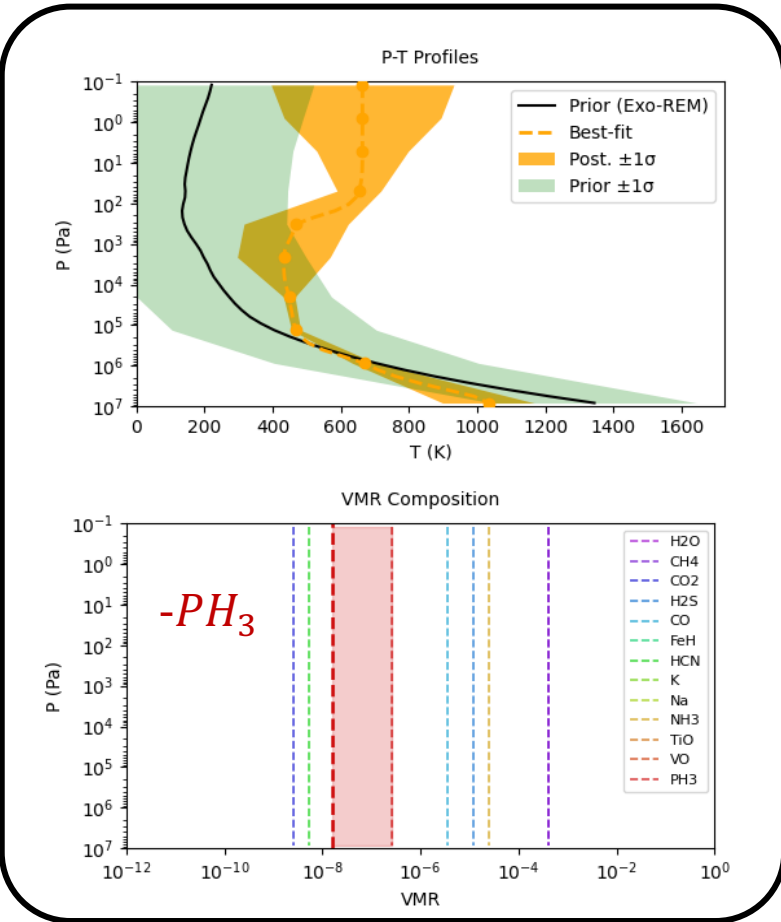
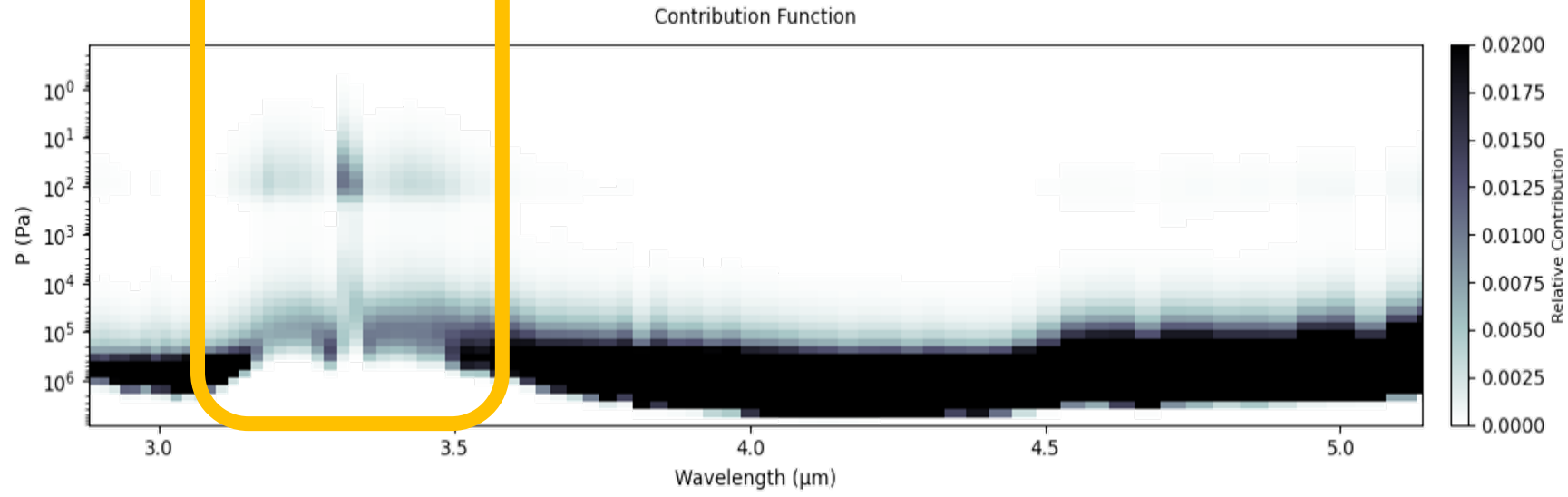
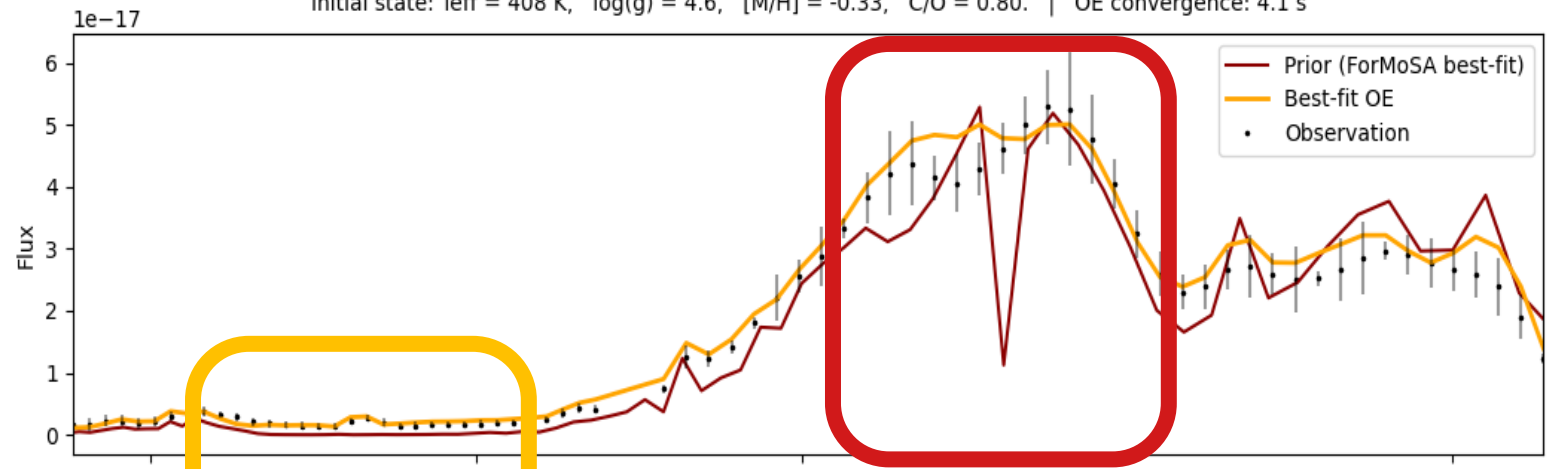
Initial state:  $T_{\text{eff}} = 408 \text{ K}$ ,  $\log(g) = 4.6$ ,  $[M/H] = -0.33$ ,  $C/O = 0.80$ . | OE convergence: 4.1 s





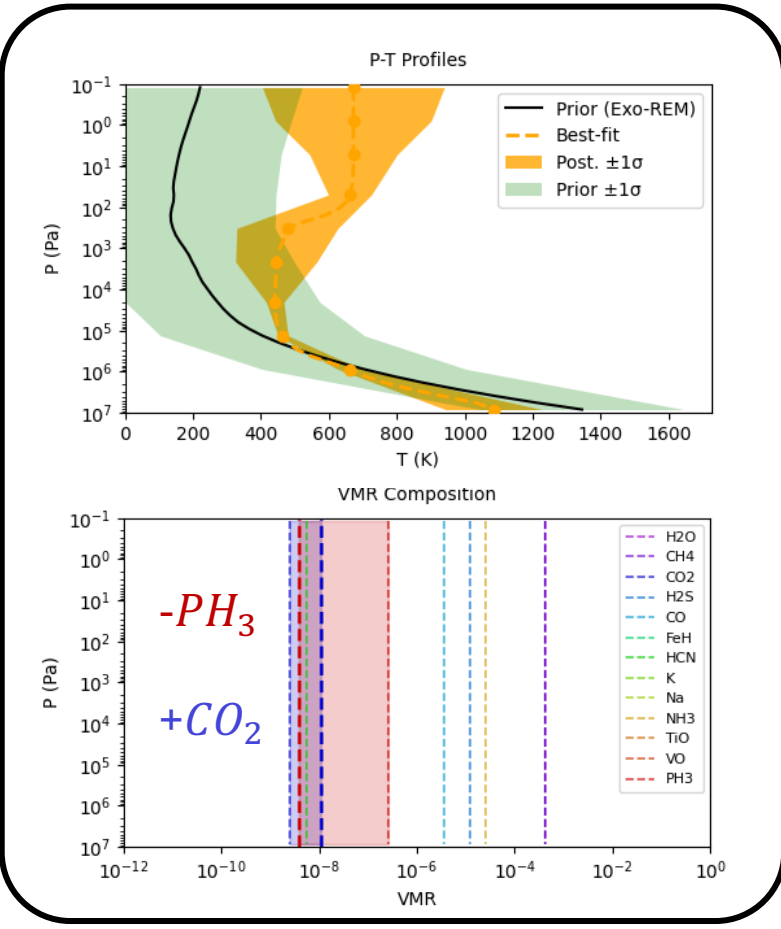
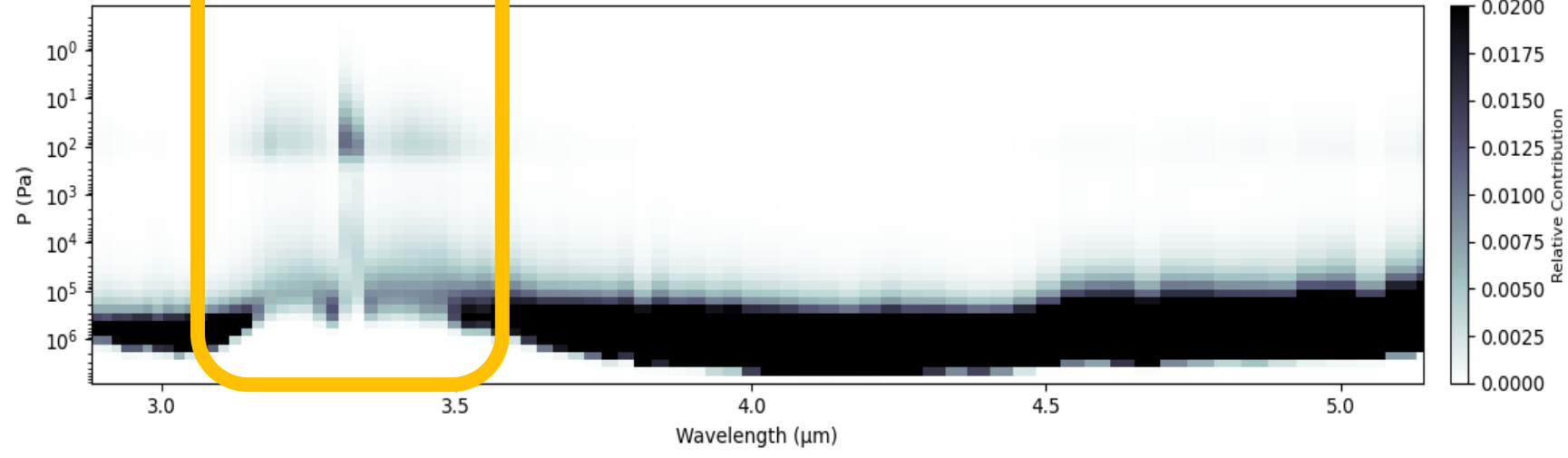
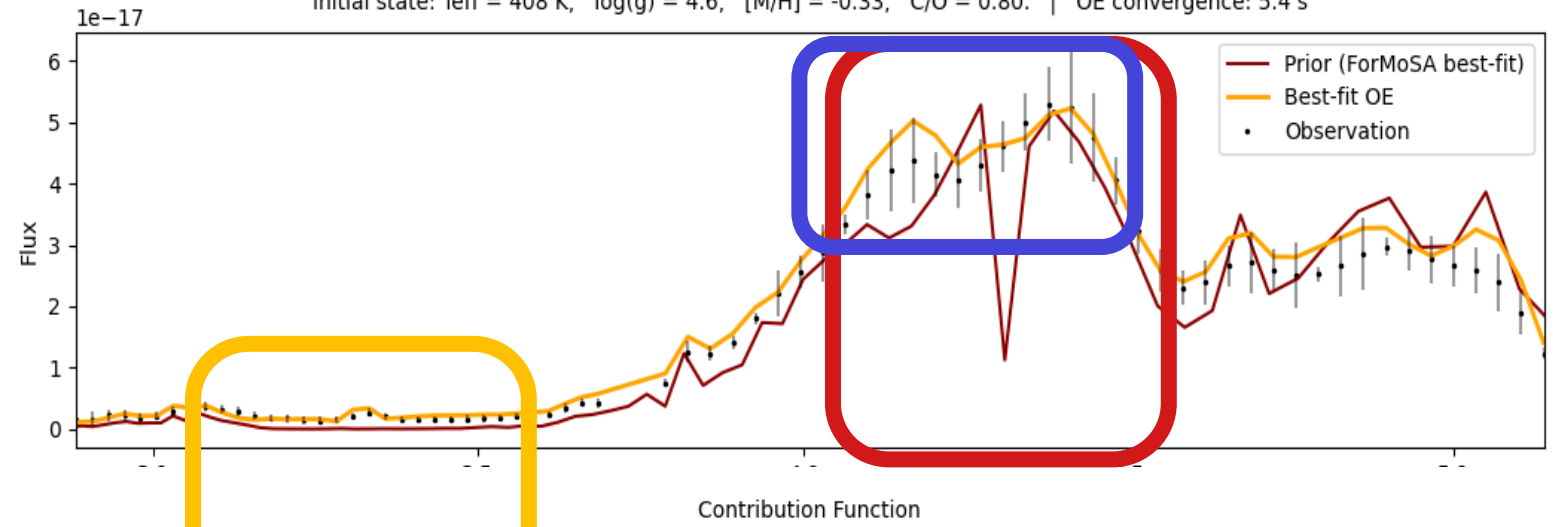
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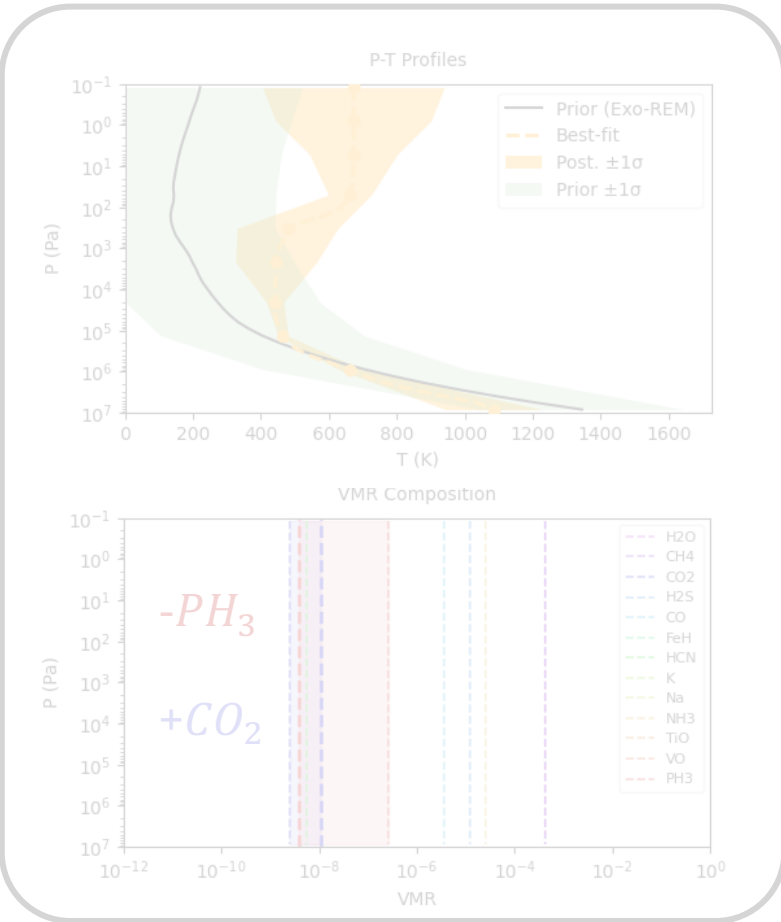


# PTEx W1935

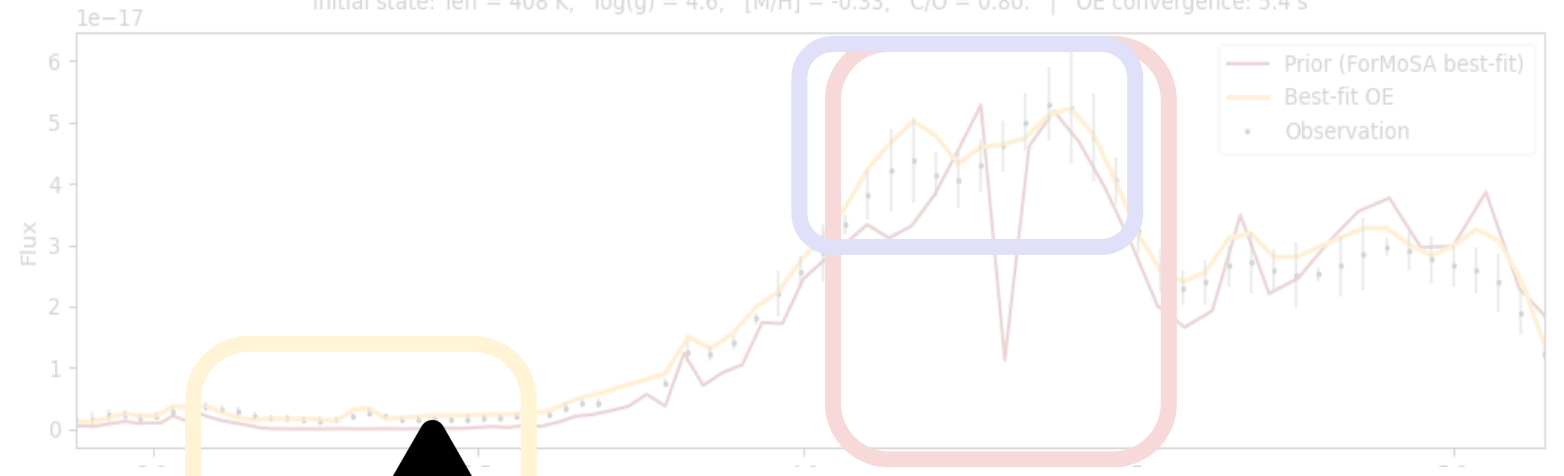
Initial state:  $T_{\text{eff}} = 408 \text{ K}$ ,  $\log(g) = 4.6$ ,  $[M/H] = -0.33$ ,  $C/O = 0.80$ . | OE convergence: 5.4 s



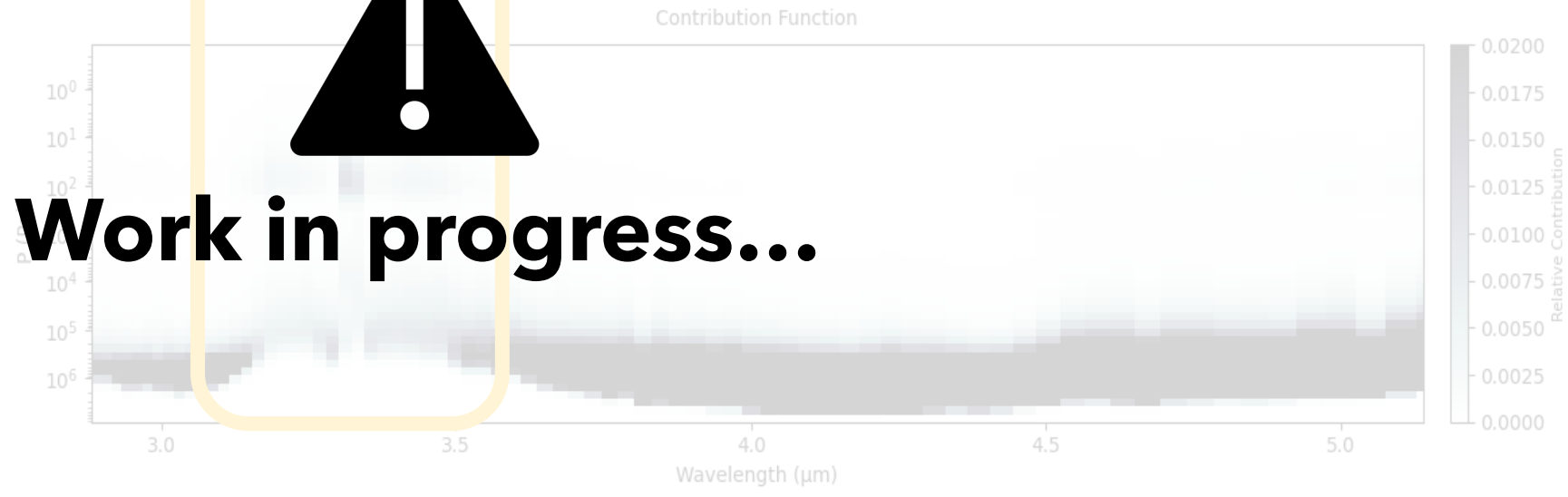
**PTEx**  
**W1935**



Initial state:  $T_{\text{eff}} = 408 \text{ K}$ ,  $\log(g) = 4.6$ ,  $[M/H] = -0.33$ ,  $C/O = 0.80$ . | OE convergence: 5.4 s



**Work in progress...**





### **Current status:**

**Validated:** Successful initial end-to-end testing

**W1935:** Selected as the ideal benchmark target

### **Prospects & preparation for future telescopes:**

**Fast and flexible retrieval:** Built for increasingly complex datasets

**Advanced physics:** Incorporating clouds, variability, reflected light, and CPDs

**New modules:** HR spectroscopy, multi-observations, and transit modules